

# Package ‘iTensor’

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**Type** Package

**Title** ICA-Based Matrix/Tensor Decomposition

**Version** 1.0.2

**Description**

Some functions for performing ICA, MICA, Group ICA, and Multilinear ICA are implemented. ICA, MICA/Group ICA, and Multilinear ICA extract statistically independent components from single matrix, multiple matrices, and single tensor, respectively. For the details of these methods, see the reference section of GitHub README.md <<https://github.com/rikenbit/iTensor>>.

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**Encoding** UTF-8

**Depends** R (>= 4.1.0)

**URL** <https://github.com/rikenbit/iTensor>

**RoxygenNote** 7.2.3

**Suggests** nnTensor, knitr, rmarkdown, testthat (>= 3.0.0)

**Config/testthat/edition** 3

**Imports** MASS, methods, graphics, utils, stats, rTensor, jointDiag, mgcv, einsum, geigen, mixOmics, groupICA

**VignetteBuilder** knitr

**NeedsCompilation** no

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**Repository** CRAN

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CorrIndex	<i>CorrIndex</i>
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### Description

Calculate the CorrIndex of the cross-correlation matrix of  $S_{true}$  and estimated  $S$ . The closer the value is to 0, the closer estimated  $S$  is to  $S_{true}$ .

### Usage

```
CorrIndex(cross_correlation_matrix)
```

### Arguments

```
cross_correlation_matrix
      Cross-correlation matrix
```

### Value

CorrIndex, which means the closeness between  $S$  and  $S_{true}$ , is returned.

### Examples

```
S_true <- matrix(runif(5*5), nrow=5, ncol=5)
S <- matrix(runif(5*5), nrow=5, ncol=5)
CorrIndex(cor(S_true, S))
```

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GroupICA	<i>Group Independent Component Analysis (GroupICA)</i>
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### Description

The input data is assumed to be a list containing multiple matrices, which share common column.

**Usage**

```
GroupICA(  
  Xs,  
  J1,  
  J2 = J1,  
  algorithm = c("pooled", "Calhoun2009", "Pfister2018"),  
  ica.algorithm = c("FastICA", "InfoMax", "ExtInfoMax", "JADE", "AuxICA1", "AuxICA2",  
    "IPCA", "SIMBEC", "AMUSE", "SOBI", "FOBI", "ProDenICA", "RICA"),  
  num.iter = 30,  
  thr = 1e-10,  
  verbose = FALSE  
)
```

**Arguments**

Xs	A list containing multiple matrices
J1	Rank parameter to decompose
J2	Rank parameter used in Calhoun2009
algorithm	Pool algorithm to merge multiple ICA results (Default: pooled)
ica.algorithm	The decomposition algorithm (Default: "FastICA")
num.iter	The number of iterations
thr	The threshold to terminate the iteration (Default: 1E-10)
verbose	Verbose option

**Value**

A list containing the result of the decomposition

**Examples**

```
X1 <- matrix(runif(100*200), nrow=100, ncol=200)  
X2 <- matrix(runif(150*200), nrow=150, ncol=200)  
Xs <- list(X1=X1, X2=X2)  
out <- GroupICA(Xs, J1=5)
```

**Description**

The input data is assumed to be a matrix. ICA decomposes the matrix and extract the components that are statistically independent each other.

**Usage**

```
ICA(
  X,
  J,
  algorithm = c("FastICA", "InfoMax", "ExtInfoMax"),
  num.iter = 100,
  thr = 1e-10,
  nonlinear_func = c("tanh", "exp", "kurtosis"),
  learning_rate = 1,
  verbose = FALSE
)
```

**Arguments**

X	A matrix
J	Rank parameter to decompose
algorithm	The decomposition algorithm (Default: "FastICA")
num.iter	The number of iteration
thr	The threshold to terminate the iteration (Default: 1E-10)
nonlinear_func	The function used in FastICA (Default: "tanh")
learning_rate	The learning rate used in InfoMax or ExtInfoMax
verbose	Verbose option

**Value**

A list containing the result of the decomposition

**Examples**

```
X <- matrix(runif(100*200), nrow=100, ncol=200)
J <- 5
out.FastICA <- ICA(X, J=J, algorithm="FastICA")
out.InfoMax <- ICA(X, J=J, algorithm="InfoMax")
out.ExtInfoMax <- ICA(X, J=J, algorithm="ExtInfoMax")
```

**Description**

The input data is assumed to be a matrix. ICA decomposes the matrix and extract the components that are statistically independent each other.

**Usage**

```
ICA2(
  X,
  J,
  algorithm = c("JADE", "AuxICA1", "AuxICA2", "IPCA", "SIMBEC", "AMUSE", "SOBI", "FOBI",
    "ProDenICA", "RICA"),
  num.iter = NULL,
  thr = 1e-10,
  r_list = NULL,
  omega_for_each_r = NULL,
  a_r_for_each_r = NULL,
  tau_list = NULL,
  num_bins = NULL,
  alpha = NULL,
  num_epoch = NULL,
  verbose = FALSE
)
```

**Arguments**

X	A matrix
J	Rank parameter to decompose
algorithm	The decomposition algorithm (Default: "JADE")
num.iter	The number of iteration
thr	The threshold to terminate the iteration (Default: 1E-10)
r_list	List of r-th order cumulants used in SIMBEC (Default: NULL)
omega_for_each_r	Weight vector of r_list used in SIMBEC (Default: NULL)
a_r_for_each_r	Parameter vector to specify the shape of partial activation function in SIMBEC (Default: NULL)
tau_list	List of lags to consider the auto-correlation used in AMUSE and SOBI (Default: NULL)
num_bins	Number of bins for histogram in ProDenICA (Default: NULL)
alpha	Learning rate used for gradient descent in RICA (Default: NULL)
num_epoch	Number of epoch used for gradient descent in RICA (Default: NULL)
verbose	Verbose option

**Value**

A list containing the result of the decomposition

**Examples**

```
ICA2
```

**Description**

The input datasets are assumed to be two matrices sharing the column space. MICA decomposes the matrices simultaneously and extracts the components that maximizes the mutual information between the components.

**Usage**

```
MICA(  
  X,  
  Y,  
  J,  
  eta = 1000 * 1e-04,  
  verbose = FALSE,  
  mu = 50 * 1e-04,  
  gamma_ts = 1  
)
```

**Arguments**

X	A matrix sharing the column space with Y (??? x N)
Y	A matrix sharing the column space with X (??? x N)
J	The rank parameter to decompose the matrices
eta	A learning rate parameter of stochastic gradient descent
verbose	Verbose option
mu	A learning rate parameter of stochastic gradient descent
gamma_ts	Weighting factor for dependence on independence

**Value**

A list containing the result of the decomposition

**Examples**

```
X <- array(runif(10*20), dim=c(10,20))  
Y <- array(runif(15*20), dim=c(15,20))  
J <- 20  
out <- MICA(X, Y, J=J)
```

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MultilinearICA      *Multilinear independent component analysis*

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### Description

#' The input object is assumed to be a Tensor object defined by rTensor package. In MultilinearICA, ICA function is performed in each mode of the tensor.

### Usage

```
MultilinearICA(  
  X,  
  Js = c(3, 3, 3),  
  modes = 1:3,  
  algorithm = c("FastICA", "InfoMax", "ExtInfoMax", "JADE", "AuxICA1", "AuxICA2", "IPCA",  
    "SIMBEC", "AMUSE", "SOBI", "FOBI", "ProDenICA", "RICA")  
)
```

### Arguments

X	An rTensor object
Js	A vector to specify the rank in each mode (Default: c(3,3,3))
modes	A vector to specify which modes are decomposed (Default: 1:3)
algorithm	The algorithm to decompose the input tensor in each mode (Default: "FastICA")

### Value

A list containing the result of the decomposition

### Examples

```
library("rTensor")  
arrX <- array(runif(10*20*30), dim=c(10,20,30))  
X <- as.tensor(arrX)  
Js <- c(2,3,4)  
out <- MultilinearICA(X, Js=Js)
```

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toyModel	<i>Toy model data for using ICA, MICA, and GroupICA There are 7 types of simulation: ICA_Type1: Time-independent sub-gaussian data ICA_Type2: Time-independent super-gaussian data ICA_Type3: Data mixed with signals having no time dependence and different kurtosis ICA_Type4: Time-dependent data ICA_Type5: Toydata to model IPCA in <math>N &lt; P</math> systems MICA: Two time-series data to model MICA GroupICA: Toydata to model GroupICA</i>
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### Description

Toy model data for using ICA, MICA, and GroupICA There are 7 types of simulation: ICA\_Type1: Time-independent sub-gaussian data ICA\_Type2: Time-independent super-gaussian data ICA\_Type3: Data mixed with signals having no time dependence and different kurtosis ICA\_Type4: Time-dependent data ICA\_Type5: Toydata to model IPCA in  $N < P$  systems MICA: Two time-series data to model MICA GroupICA: Toydata to model GroupICA

### Usage

```
toyModel(model = "ICA_Type1", seeds = 123)
```

### Arguments

model	"ICA_Type1", "ICA_Type2", "ICA_Type3", "ICA_Type4", and "ICA_Type5", "MICA", and "GrouICA" are available (Default: "ICA_Type1").
seeds	Random number for setting set.seeds in the function (Default: 123).

### Value

A list containing simulation data sets.

### Examples

```
data1 <- toyModel("ICA_Type1")
data2 <- toyModel("ICA_Type2")
data3 <- toyModel("ICA_Type3")
data4 <- toyModel("ICA_Type4")
data5 <- toyModel("ICA_Type5")
data6 <- toyModel("MICA")
data7 <- toyModel("GroupICA")
```



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